

Constraints for 3D Graphics on the Internet

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Abstract

In this paper we present a flexible extension to support constraints in VRML97, the standard for interactive 3D graphics on the internet. After a short introduction to the dynamic concepts of VRML97, we discuss the design rationale of our extension and explain its implementation. In particular we look at how the extension is integrated into the initialization process and the rendering loop of a VRML browser, the software which loads and displays VRML scenes. So far, we implemented solvers for one-way equational and finite domain constraints, but our architecture allows to easily add other constraint solvers.

Keywords: computer graphics, world-wide-web, one-way equational constraints, finite-domain constraints

1 Introduction

VRML has become the standard for providing 3D content on the internet. VRML was designed to be declarative, but the way program code is added does destroy this declarativity. Constraints can remedy this situation and increase the potential for visual authoring and visual programming. Our extension allows to separate constraints and solvers, thus allowing constraints to become part of the VRML file. The architecture described in this paper makes it possible to add other kinds of constraints, e.g. non-linear constraints, by taking care of the integration into the interactive, real-time graphics framework of VRML. Thus, to constraint programmers it opens up a wide area of emerging applications on the internet including 3D modeling, simulation and gaming as well as 3D e-commerce.

This paper focusses on the implementation aspects of the extension and in particular on the challenging task of properly integrating constraint solving into the event processing and rendering loop. As we use established constraint solving methods these are only described to the extent to which it is required to illustrate the integration. Ideally, the discussion should motivate and enable others to apply their constraint solvers to virtual worlds on the internet.

1.1 Constraints in Computer Graphics

Constraints have been used for user-interfaces since the Sketchpad system [13] in 1963. Constraints enforce hidden relations between objects as they are common in layouts or animations. For example several kinds of 2D animations can be expressed as constraints in Amulet [10], and there exists a constraint-based sys-

tem to visually construct 3D animations [9]. In fact many animation techniques in the literature, e.g., inverse kinematics, morphing, rocking, particle systems, are specified by sets of constraints, then one or more variables are manipulated over time. The animation is produced as the constraint solver tries to satisfy the constraints by computing the properties of the graphic objects. Constraints are also a powerful tool for modeling [8, 15] and visual programming [2]. In distributed systems they provide a concise way to encode communication and synchronization [1].

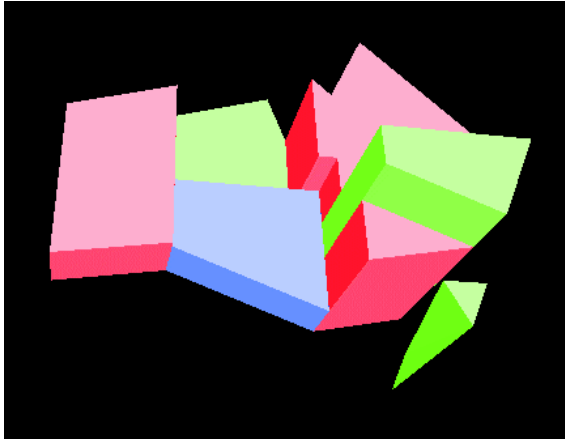
1.2 Extending the VRML97 standard

VRML has evolved from a description language of a static scene graph (VRML 1.0 in 1995) to a modeling language for 3D worlds including behavior, animations, and user interaction (VRML 2.0 in 1996,[3]). A revised specification of VRML 2.0 has become an official ISO Standard called VRML97 [14]. From a programming language designer's point of view VRML lacks many features which have proven useful for specifying algorithms. As VRML was primarily designed with the intention to specify 3D objects and their behavior, we have to be careful when we try to transfer programming language concepts to VRML.

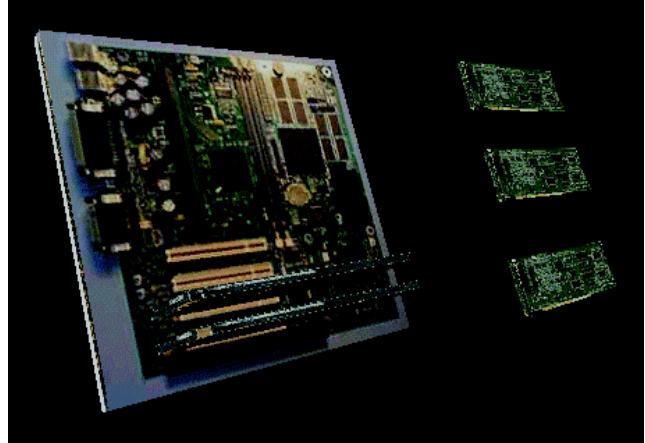
Previously we have designed a language called VRML++ [5, 6], which extends VRML by classes, inheritance and an improved type system and introduces the concept of dynamic routing. The current paper addresses the design and implementation issues of extending VRML by constraints. Constraints make VRML more expressive. They ease specification of animations and of layout and interaction in user-interfaces.

Applications implemented with our exten-

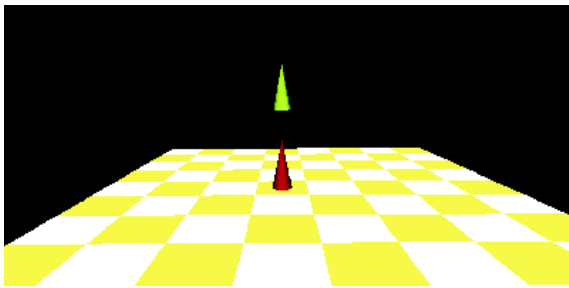
N-Colors



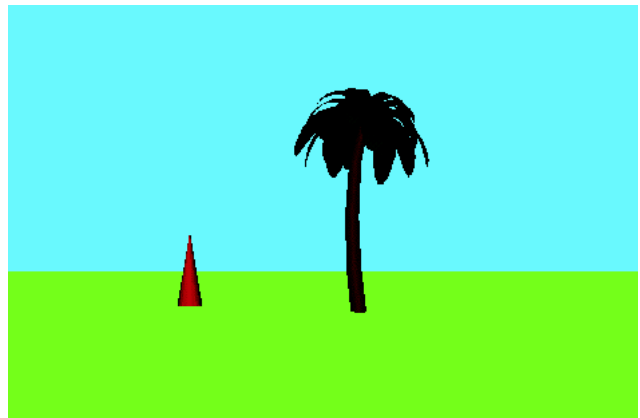
Computer Configuration



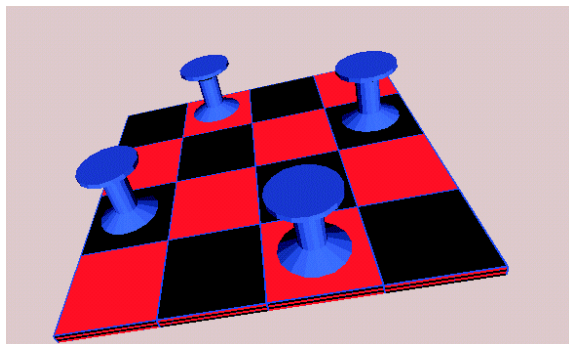
Navigation



Collision Detection



N-Queens



Multiway Constraints

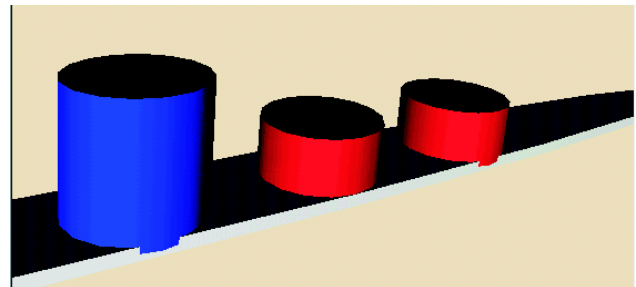


Figure 1: Some applications implemented with VRML and constraints

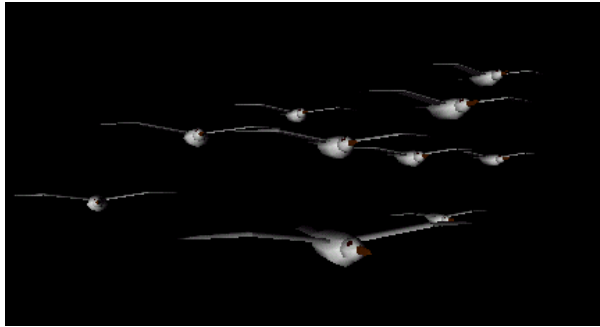


Figure 2: Flocking

sion include navigation, collision-detection, configuration and animation (see Figure 1) and have been described in a previous paper [7], which targets a computer graphics audience. As an example of these applications Figure 2 shows an event-based implementation of flocking [11]. Below the definition of the constraints using the extension we introduce in this paper is given. Every bird in a flock of n birds gets a constraint encoding its dependency on itself and the remaining $n - 1$ birds:

```
DEF constr Constraint {
  startEval TRUE
  inames [ "b1", "b2", "b3" ]
  inodes [ USE bird1,
           USE bird2 ,
           USE bird3 ]
  constraints [
    "b1.translation=
      Follow(b1.translation,
             b2.translation,
             b3.translation) "
    "b2.translation=
      Follow(b2.translation,
             b1.translation,
             b3.translation) "
    "b3.translation=
      Follow(b3.translation,
             b1.translation,
             b2.translation) "
  ] }

```

2 Dynamic Features of VRML: Routes and Scripts

As we want to extend VRML, we first have to look at what is there in VRML.

The part of the software which creates an image from a description of a scene, its objects and light sources and the viewer is called the renderer. In most 3D graphics systems the description is represented as a graph, called the scene graph. The renderer traverses this graph and accumulates the information contained in the nodes along each path. This information includes transformations, colors and geometric data. As the scene graph is usually a directed acyclic graph and not just a tree, a node can be reached on different paths, i.e. it has to be evaluated in different contexts.

For computer animations the render loops:

1. Change the scene graph or values in the scene graph.
2. Render the scene.

In classical 3D systems the scene graph was built as part of the program code, that is, it was integrated into the system. Using VRML a scene graph can be specified independently of a specific implementation of a graphics system. The constructs of VRML are called nodes, because they specify a scene graph. A node contains fields, which correspond to the edges of the graph. A node is defined by its node type and values for its fields. These values can be nodes again. There are default values of each field and each field may only take values of a certain type. The syntax to define a node is as follows:

Type { *field*₁ *value*₁ ... *field*_{*n*} *value*_{*n*} }

For example `Box { size 1 2 1 }` defines a node of type `Box` and its field `size`

has the value 1 2 1, i.e. a box with 1m, height 2 m and depth 1m is defined.

Actually, there are three kinds of fields: field, eventIn and eventOut. Pure fields are used to store data, while an eventIn receives data and an eventOut sends data along a route. A route connects an eventOut to an eventIn. If an eventOut is connected to an eventIn, then the value of the eventIn changes, whenever the value of the eventOut changes. An efficient implementation of routes is described in [16].

In VRML there are some special nodes which produce eventOuts, these include TouchSensor nodes which produce an event, when the user clicks at an object and TimeSensor nodes, which periodically produce eventOuts.

For example, a node of type TimeSensor periodically produces an eventOut named fraction_changed.

```
DEF CLOCK TimeSensor { ... }
```

This eventOut can be sent to other nodes, e.g., an interpolator node of type PositionInterpolator.

```
DEF PI  
  PositionInterpolator { ... }
```

Depending on the value received as eventIn set_fraction this node computes a position in 3D space as eventOut value_changed. This eventOut can be sent as a set_translation eventIn to a node of type Transform. What eventOut is sent to which eventIn is defined with the ROUTE primitive. It statically wires routes between nodes. Note, that the names CLOCK, PI and CYL have been bound to instances using DEF above. At run-time the scene graph can be changed by sending values along the routes.

```
ROUTE CLOCK.fraction_changed  
  TO PI.set_fraction  
ROUTE PI.value_changed  
  TO CYL.set_translation
```

In our example, the objects defined as children of the Transform node change their position in the course of time. What we just described is the basic mechanism to program animations in VRML.

In VRML97 it is also possible to add programs in languages like JavaScript, VRMLScript or Java to the 3D objects in a file. Such program code is attached to nodes of type Script. Execution of this code is triggered by events. Using JavaScript for each eventIn of a Script node a function with the same name as the eventIn has to be defined. The function takes the value of the eventIn as argument. Within the function new values can be assigned to eventOuts of the Script node or to eventIns of other nodes. These other nodes will then react accordingly to these changes. Note, that in this way it is possible to change an eventIn of a node without using a route. The implementation of script nodes using Java differs from the above and is described in the section “Java Scripting API” of the VRML97 specification [14]. In particular, the API provides the methods getValue() and setValue() to read and write events.

As an alternative to Script nodes VRML97 also provides the so-called External Authoring Interface EAI. The EAI allows applets to call methods of the VRML browser and vice versa.

3 Design Rationale

Our final goal is that constraints become an integral part of the VRML language. The first step to achieve this is to provide an extension

of VRML97 such that we and others can experiment with different flavors of constraints.

A first effort to implement constraints on top of VRML with the help of a preprocessor turned out to be too restrictive and was heavily depending on the routing mechanism of a particular browser [4]. At a workshop at VRML98 Richard presented an implementation where constraints had been hard coded in a constraint solver in Java to control a VRML scene [12].

In our approach constraints and solver are separated and constraints are part of the VRML file. To achieve this we implemented a prototype Constraint. It encapsulates constraint solvers in a Script node. The solvers are programmed in Java. The constraints are passed as strings to the Script node.

```
EXTERNPROTO Constraint [
  field MFString inames
  field MFString innodes
  field MFString protoField
  field MFString protoType
  field MFString domains
  field MFString domainDefs
  field MFString userFunctions
  field SFFloat startEval
  field SFFloat eventFirstPriority
  field MFString constraints
] "ProtoConstraint.wrl#Constraint"
```

Some of the fields of the Constraint prototype are only needed as work arounds for missing functionality of the Java Scripting API, so we do not explain them here, but they are described in [7].

The fields domains and domainDefs are used to define the domains for finite domain constraints.

The field userFunctions offers the possibility to add any needed function to the constraint solver and use these functions in the constraints. The syntax needed to support this

feature is very easy: First, the user has to define the signature of the function and then the function can be defined in JavaScript syntax. The signature consists of the return type, the function name and the parameter types.

If the field eventFirstPriority is TRUE, a variable which was changed by an event and triggers the constraint solver can not be set to a different value by the constraint solver.

Finally, the field constraints contains a list of strings (MFString), each string represents a constraint. The constraints are interpreted as one-way equational constraints if domains and domainDefs are empty and as finite domain constraints, otherwise.

Constraints are of the form *path relop expression* where *path* identifies a field in the scene graph, *relop* is a relational operator and *expression* is either a constant of primitive type like MFInt32, a value of a field or a function, see grammar below:

```
constraint  → path relop expression
relop       → = | != | <= | >= | < | >
expression  → path
              | functionname ( path* )
              | constant
path        → nodename.tail
tail        → fieldname | fieldname [ int ]
              | tail.tail
```

The following is an example of a constraint, which relates the value of a field radius of type SFFloat to the second value in a field size of type SFVec3f:

```
CAR.children[2].radius
= Add( SLIDER.size[2], 10)
```

Assume that you want to position an object A between two objects B and C and that you have written a function middle(p, q) which computes the mid point between two points p

and `q`. In VRML for the function we have to create a Script node `S` and then we have to add the following routes:

```
ROUTE B.translation_changed
  TO S.set_p
ROUTE C.translation_changed
  TO S.set_q
ROUTE S.result
  TO A.set_translation
```

Using constraints we can just write:

```
A.translation
  = middle(B.translation,
           C.translation)
```

This is not just shorter, but it is also more readable, accessible and maintainable. More examples including the VRML source code can be found in a previous paper [7].

4 Implementation

Figure 3 shows the scene graph, routes and dependency graph of the first example constraint above. The dependency graph is built by a Java program which is encapsulated in the `Constraint` node in the scene graph. To better understand the relation of the scene graph and the dependency graph as well as how the constraint solvers work, we look at the steps performed by the initialization process and the rendering loop of a VRML browser and what additional steps are added by our extension.

4.1 Initialization

During initialization the VRML browser performs the following three steps:

1. Load VRML file, parse it and build scene graph including script nodes.

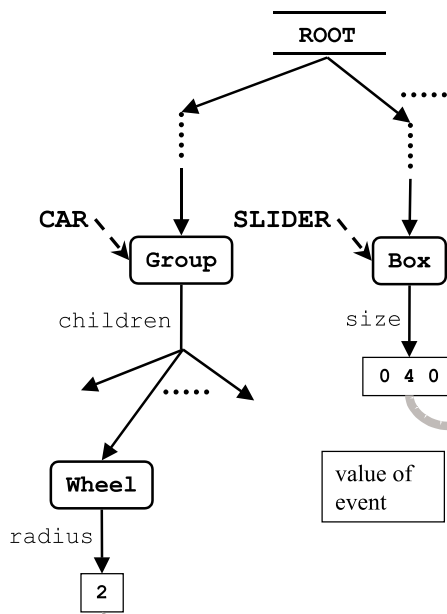
2. Connect all routes.

3. Call method `initialize()` of each script node.

In the last step also the method `initialize()` of the script in the `Constraint` prototype is called. It parses the string contained in its field `constraints` and creates a dependency graph. A node in the dependency graph represents a variable in the constraints and contains an attribute `outofdate`, which indicates, that its value of this variable is valid or not. It contains a list dependencies of nodes representing variables which depend on this variable and it contains a list constraints of objects representing single constraints. These objects contain the variable, a relational operator and a tree representing the expression in the constraint. Finally, each node in the dependency graph has two flags which are needed because not all fields referenced in the paths of a constraint must exist at all times. The flag `nodeActive` is false if the VRML-node to which the field belongs does not exist at initialization or whenever it is removed. The flag `constraintActive` is false, whenever the flag `nodeActive` of this node or a node it depends on is false. As a result, when a constraint is not active the constraint solver will not try to solve it. But as soon as all variables referenced in the constraint exist, it will become active and thus be solved.

For each variable in the constraints it creates a script node which receives the value of the variable and sends the name of the variable to the script node of the `Constraint` prototype. For this, additional routes are added to the scene graph. We need an intermediate node for each variable, because in case of fan-in, i.e. if several variables send their modified values to the script, the script node can not identify the sender of each value, it just receives the value.

Scene Graph



Dependency Graph

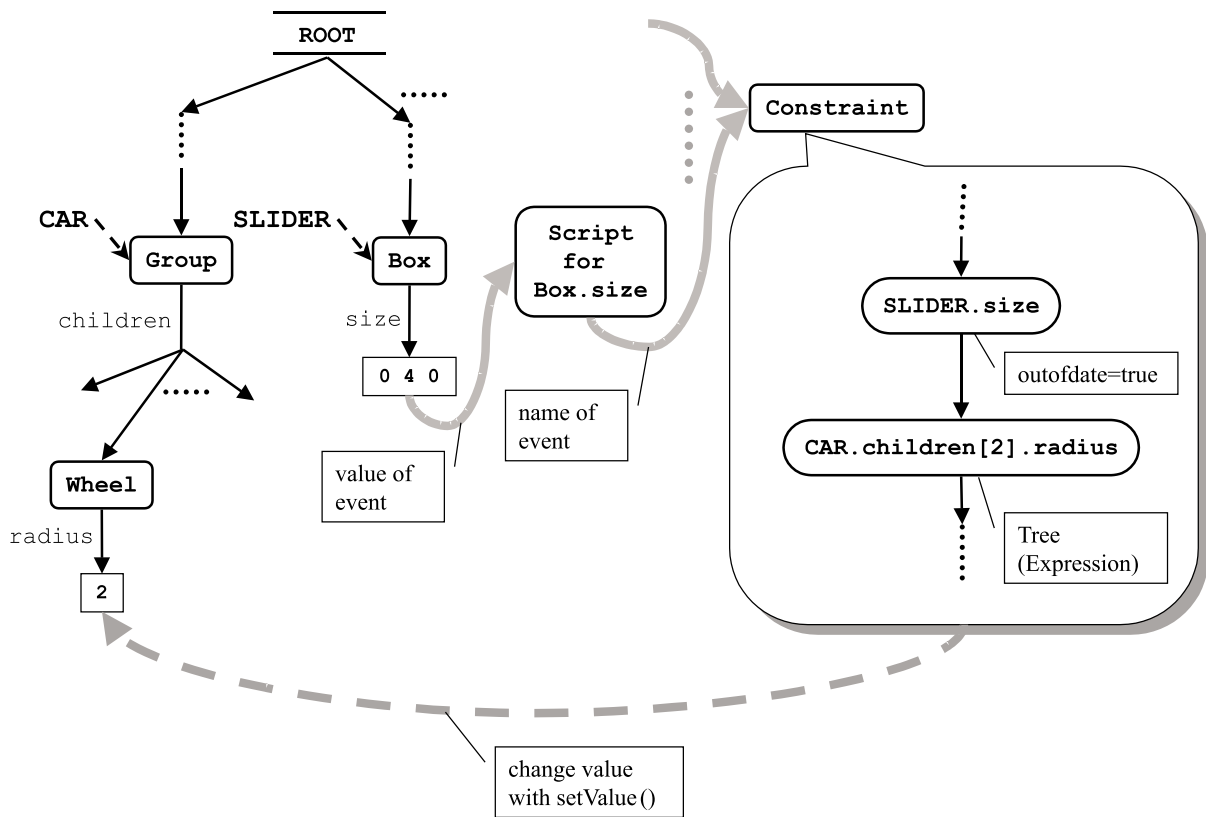


Figure 3: Relation of scene graph and dependency graph

But if the script receives the name of the variable, it can access the value with the method `getValue()` of the Java Scripting API.

For each user-defined function the method `initialize()` of the `Constraint` prototype adds a script node, which encapsulates that function, to the scene graph as we will explain in the next section.

If the field `startEval` of the `Constraint` prototype is `TRUE`, also the constraint solver is invoked during this initialization process.

4.2 Rendering Loop

After initialization the VRML browser executes the following loop [16]:

1. Process events which are caused externally like mouse clicks and clock ticks.
2. Route the messages
3. Evaluate scripts and interpolators and propagate events they cause. By using timestamps or similar techniques the browser postpones the handling of events which are changed more than once during one iteration to the next iteration.
4. Update the scene graph based on the events that occurred since the last rendering
5. Render the scene

If the value of a field which is a variable in the constraints changes, an event occurs and in step 3 of the above loop the constraint solver is invoked. It gets the names of all variables which changed since the last frame rendered and sets the attribute `outofdate` of these variables in the dependency graph to `false`.

4.2.1 One-way equational constraints

To solve one-way equational constraints we use an extension of the algorithm by Zanden et al. [17] for constraints with pointer variables. In particular, we added activation and deactivation of constraints to allow dynamic adding and removing of nodes. As in their algorithm the constraint solver has two phases. In the nullification phase all variables are marked as `outofdate` which depend on a variable which has become `outofdate`. In the re-evaluation phase the values of all variables are recomputed recursively. Let k be the dependency graph node whose value changed:

```
if (eventFirstPriority==false)
    eval(k)
else
    for each d ∈ k.dependencies
        do eval(d)
```

In the second case only the values of all depending variables are recomputed. Here is the definition of the function `eval()`.

```
eval(k) = {
    if (k.isoutofdate
        and k.activeNode
        and k.constraintActive)
    { k.outofdate=false;
      for each c ∈ k.constraints
          do c.solveConstraint();
      for each d ∈ d.dependencies
          do eval(d); } }
```

where `solveConstraint()` computes the value of the expression in the constraint.

4.2.2 Adding and removing nodes

In VRML it is possible that nodes can be added or removed dynamically from the scene graph by using the events `addChildren` and `deleteChildren`. As a result, in a path like `CAR.children[2].radius` the node referenced by `CAR.children[2]` might cease to exist or might be added later. To cope with this situation routes are added from each `children` field in a path to the eventIn `childrenControl` of the script in the `Constraint` prototype. The value of the event is the partial path for this field, e.g. `CAR.children`. The script can now activate or deactivate the according node in the dependency graph and all nodes depending on it.

4.2.3 User-defined functions

To implement user-defined functions we had two alternatives: create a script node for each use of such a function in a constraint or create a script node for each function defined. The structure and protocol of the first solution would have been less complex, but it would have increased the number of script nodes in the scene graph considerably. Thus we chose the second solution. Consider the following example where we implement a function `EqualY(p,q)` which returns `true` if the Y-coordinate of the two points `p` and `q` are equal:

```
Constraint { ...
    userFunctions
    [ "SFBool
      EqualY(SFVec3f, SFVec3f) "
      "function eqy(x1, x2)
        { return x1[1]==x2[1]; } "
    ]
    ... }
```

At initialization the Constraint prototype will create the following script node from the above specification:

```
Script {
  eventIn SFVec3f set_p1
  eventIn SFVec3f set_p2
  eventIn SFBool UpdateResult
  field SFVec3f p1 0 0 0
  field SFVec3f p2 0 0 0
  eventOut SFBool ResultUpdated
  eventOut SFBool result
  url [
    "vrmlscript:
      function set_p1(value)
        { p1=value; }
      function set_p2(value)
        { p2=value;
          result=eqy(p1, p2);
          ResultUpdated=true; }
      function UpdateResult(value)
        { ResultUpdated=false; }
      function eqy(x1, x2)
        { return x1[1]==x2[1]; }"
  ]
}
```

To evaluate an occurrence of the function `EqualY(p, q)` in a constraint, the constraint solver (in the method `solveConstraint()`), will perform the following steps:

1. Set eventIn `UpdateResult` to false.
2. Set eventIn `set_p1` to the value of p .
3. Set eventIn `set_p2` to the value of q . Then the function `set_p2()` performs the test and sets the flag `ResultUpdated` which is used for synchronization of the script node for the function `EqualY()` and the constraint solver, because these are running concurrently.

4. Wait until the flag `ResultUpdated` becomes true, then read the value of the eventOut `result`.

4.2.4 Finite domain constraints

For finite domain constraints we have to make sure that all constraints are satisfied before the last step in the rendering loop, such that no inconsistent scene is rendered. For this, we have a copy of the value of each field in the dependency graph and after all constraints have been solved these values are written to the scene graph at once. Our FDC solver uses backtracking with domains sorted by size (first fail principle).

4.2.5 Technical Remarks

We would have liked to add a keyword parent for paths in the constraints. Unfortunately the Java Scripting API does not provide a way to access the parent or one of the parents of a node. The only workaround we came up with was to mirror the whole scene graph and process all events additionally in Java, which would considerably degrade the performance.

Speaking of performance, we found that the Java Scripting API is the major bottleneck in our implementation. The problem is that the value of a field is set by method calls instead of assignments. We found that setting the value of an object of class `SFVec3f` with `setValue()` it is about 300 times slower than assigning the value to a float array of size three which would be an equivalent, but more efficient representation. If the `SFVec3f` object is actually a field in the scene graph, the access is another 20% slower. Fortunately, we did not use the External Authoring Interface EAI and implement the constraint solver as an applet. For the EAI we measured that calls to `setValue()` are even 20.000 times slower

than assignments to float arrays.

5 Conclusion

Applications of constraints for 3D computer graphics on the internet include navigation, collision-detection, configuration and animation. Constraints capture the required knowledge in a declarative way and thus increase maintainability of such applications. We feel that constraints provide a powerful, expressive and natural way to specify dependencies between fields of different nodes and that they should replace or extend routes in a future VRML standard. We have shown how constraints can be integrated into the initialization process and the rendering loop of a VRML browser. The whole extension was designed such that it is easy to add other constraint solvers as they only work on the dependency graph. There should be no need to change the parser, the communication with the VRML scene and the handling of user-defined functions. As part of our future research we want to investigate how to combine our previous work on VRML++ with that on constraints.

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